

# Year 12 T6

## Maths Overview

### Number & Algebra

Learning Outcomes	Elaboration	Textbook
<p>Students should be able to:</p> <ul style="list-style-type: none"> <li>• use surds and <math>\pi</math> in exact calculations;</li>   <li>• Change a recurring decimal to a fraction;</li>   <li>• distinguish in meaning between the words <i>equation</i>, <i>formula</i>, <i>identity</i> and <i>expression</i>;</li>   <li>• derive a formula, substitute numbers into a formula and change the subject of a formula, including cases where the subject appears in more than one term or where a power of the subject appears;</li>   <li>• solve linear inequalities in one or two variables, and represent the solution set on a number line or suitable diagram;</li>   <li>• find the intersection points of the graphs of a linear and quadratic function, knowing that these are the approximate solutions of the corresponding simultaneous equations</li> </ul>	<p>Distinguish between rational and irrational numbers; know that <math>\sqrt{2}</math> and <math>\pi</math> are irrational.</p> <p>Simplification of surds including rationalise a denominator;</p> $\sqrt{12} = 2\sqrt{3}; \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3};$ <p>Write <math>(5 - \sqrt{5})^2</math> in the form <math>a + b\sqrt{5}</math>.</p>	<b>16</b>
	<p>Know the significance of recurring and non-recurring decimals.</p>	<b>13</b>
	<p>Calculate with numbers in standard index form using both positive and negative powers of ten.</p> <p>Calculate <math>\frac{3.2 \times 10^4}{1.6 \times 10^{-3}}</math>;</p> <p>Use standard index form on a calculator.</p>	<b>16</b>
	<p>Know the meaning of and use the word 'identity'.</p> <p>Understand the identity symbol.</p>	
	<p>Use the formula <math>F = \frac{GMm}{r^2}</math> to calculate one variable given the others.</p> <p>Transform formulae such as</p> $v = u + at, \quad A = \pi r^2,$ $p = \frac{100(s - c)}{c}$	<b>15</b>
	<p>List the values of the integer <math>n</math> such that <math>-10 &lt; 2n \leq 20</math> or solve the inequality <math>2n - 3 \geq 7</math> illustrating the solution on a number line. Solve <math>x \leq 3x - 5</math> where <math>x</math> is a real number.</p> <p>Use straight line graphs to locate regions representing linear inequalities; For example, <math>x &lt; 10, y \geq 6, y &lt; 2x + 3</math>.</p>	<b>14</b>
	<p>For example, Solve <math>y = 5x - 6</math> and <math>y = x^2</math>, by drawing the graph of each function. Use the graph of <math>y = x^2 + 5x</math> to solve <math>x^2 + 5x = 7</math></p>	<b>19, 35</b>

<p>representing the linear and quadratic functions;</p> <ul style="list-style-type: none"> <li>draw, sketch and recognise graphs of: <ul style="list-style-type: none"> <li>simple cubic functions;</li> <li>the reciprocal function</li> </ul> <math display="block">y = \frac{1}{x} \text{ with } x \neq 0;</math> </li> <li>the function <math>y=k^x</math> for integer values of <math>x</math> and simple positive values of <math>k</math>; and</li> <li>the trigonometric functions <math>Y= \sin X</math>, <math>Y= \cos X</math> and <math>Y= \tan x</math></li> <li>construct the graphs of simple loci;</li> <li>construct linear, quadratic and other functions from real-life problems and plot their corresponding graphs; use growth and decay rates and display these graphically; and</li> <li>use index laws in algebra for multiplication and division of integer, fractional and negative powers.</li> </ul>	<p>Make tables of such functions, sketch and interpret their graphs using graphical calculators and computers to understand their behaviour. To include drawing graphs of:</p> $y = ax + b$ $y = ax^2 + bx + c$ $y = \frac{a}{x} \text{ where } a \neq 0 \text{ and } x \neq 0$ $y = a^x \text{ where } a = 2, 3, 4$ <p>Use the graphs of <math>y = x^2 + 5x</math> and <math>y = x^3</math> to solve <math>x^3 = x^2 + 5x</math></p> <p><math>y = a^x</math> where <math>a = 2, 3, 4</math> Use the graphs of <math>y = x^2 + 5x</math> and <math>y = x^3</math> to solve <math>x^3 = x^2 + 5x</math></p> <p>Recognise the characteristic shapes of these functions. Within the range <math>0^\circ</math> to <math>+ 360^\circ</math></p> <p>Including the region bounded by a circle and an intersecting line.</p> <p>For example, distance-time graphs including intersecting travel graphs. Know about rates of economic growth and decline and the half-life of radioactive elements.</p> <p><b>Simple expressions such as</b></p> $6x^6 \div 3x^4, 2x^2 \times 3x^3, (3x^2)^3;$ $\frac{6x^2y}{8xy^3} \quad \frac{2x^4}{y} \times \frac{-3y^2}{6x^2}$ <p>Use :</p> $x^0 = 1, y^{-3} = \frac{1}{y^3}, \frac{x^2}{x^3} = \frac{1}{x} = x^{-1}, x^{\frac{1}{2}} \times x^{\frac{3}{2}} = x^2$	<p><b>35</b></p> <p><b>33, 36</b></p> <p><b>29</b></p> <p><b>19, 20</b></p> <p><b>16, 20</b></p>
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